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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

Fourth Semester B.Tech Degree Examination July 2021 (2019 Scheme)

Course Code: MAT202 Course Name: PROBABILITY, STATISTICS AND NUMERICAL METHODS

METHODS Max. Marks: 100 **Duration: 3 Hours** (Normal distribution table and t- distribution table are allowed) PART A (Answer all questions; each question carries 3 marks) Marks 1 Determine the binomial distribution for which mean is 4 and variance is 3. 3 2 X follows Poisson distribution with mean 6. Find P(X = 1), Variance (X). 3 A continuous random variable X has PDF $f(x) = \frac{k}{1+x^2}$; $-\infty < x < \infty$ 3 3 (ii) $P(X \ge 0)$ Determine (i) *k* 4 A random variable X follows exponential distribution with mean 3. Find 3 P(X > 3), Variance(X)5 The proportion of a characteristic of a population is p = 0.37. Find the mean 3 and variance of the sample proportion obtained from a sample of size 100. 6 A sample of size 49 is taken with mean 35 and standard deviation 11 from a 3 population. Find the 99% confidence interval for the population mean. Use trapezoidal rule to evaluate $\int_0^1 x^3 dx$ considering five subintervals. 7 3 8 Find a root between 0 and 1 for cosx = 3x - 1 using Newton-Raphson 3 method correct to 3 decimal places. 9 3 Use Rungi-Kutta method of second order to find y(0.1) for $\frac{dy}{dx} = \frac{y^2 - x^2}{v^2 + x^2}$, v(0) = 1. (Take h = 0.1) 10 Given $\frac{dy}{dx} = 1 - y$, y(0) = 0. Use Euler's method with h = 0.1, to compute 3 the value of y(0.2). **PART B** (Answer one full question from each module, each question carries 14 marks) Module -1 11 a) The pdf random variable X is given 7 of below. Find k, P(X < 4), E(X), Var(X).

1 2 3 4 5 6

9k

11*k*

13*k*

7k

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5k

3k

k

f(x)

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b) Prove that binomial distribution can be approximated to Poisson distribution when n is large, p is small and $np = \lambda$.

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- 12 a) A gambler plays a game of rolling a die with the following rules. He will win Rs. 200 if he throws a 6, but will lose Rs. 40 if he throws 4 or 5 and lose Rs. 20 if he throws 1, 2 or 3. Find the expected value that the gambler may gain.
 - b) The joint distribution of (X, Y) is given by $f(x, y) = \frac{x+y}{21}$, x = 1,2,3 and y = 1, 2. Then find the marginal distributions. Also, find E(X), E(Y).

Module -2

- 13 a) In an examination, 30% of the students got marks below 40 and 10% got 7 marks above 75. Assuming the marks are normally distributed find, the mean and standard deviation of the distribution.
 - b) Buses arrive at a specified stop at 15 minutes interval starting at 8 am. If a passenger arrives at the stop at a random time that is uniformly distributed between 8.00 and 8.30 hours, find the probability that the passenger waits (i) less than 6 minutes for the bus (ii) at least 12 minutes for the bus.
- 14 a) A distribution with unknown mean μ has variance 1.5. Use Central Limit 7 Theorem to find, how large a sample should be taken from the distribution in order that the probability that the sample mean will be with in the 0.5 of the population mean is 0.95.
 - b) The joint PDF of (X, Y) is given by f(x, y) = kxy 0 < x < 4; 1 < y < 5 7 = 0 elsewhere Find value of k. Determine marginal pdf of X and Y. Evaluate $P[X \ge 3, Y \le 1]$

2]. Check whether X, Y are independent?

Module -3

- 15 a) A sample of 20 items has mean 42 and SD 5. Test whether the sample is from a population with mean 45? (5% level of significance)
 - b) The mean life time of certain products is 1800 hrs with SD of 100 hrs. By applying a new technique, it is claimed that the mean life has increased. To test the claim a sample of 50 products were taken and it is found that the mean life time is 1850 hrs. Can we support the claim at 1% level of significance?
- 16 a) In a university 325 out of 600 students are boys. Does this information support the conclusion that majority of students in this university are boys? (use 5% level of significance)
 - b) Random samples drawn from two countries gave the following data relating to 7 height of adult males.

	Country A	Country B
Mean height	67.42	67.25
Standard deviation	2.58	2.50
Number in samples	1000	1200

Is the difference between the means significant? (5% level of significance)

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Module -4

17 a) The population of a town in the census is as given in the data. Estimate the population in the year 1996 using Newton's backward interpolation formula.

Year (x):

Population (y):

1961 46 1971 66 1981 81 1991 93 2001 101 7

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b) Using Lagrange's Interpolation method, find the polynomial f(x) which agree with the following data: f(1) = 1, f(3) = 27, f(4) = 64. Hence find f(2).

18 a) Using Newton's divided difference interpolation formula evaluate f(3) from the following table:

C	,					
	x	1	2	4	5	6
	у	14	15	5	6	19

b) Evaluate $\int_0^1 \frac{1}{1+x^2} dx$ using Simpson's 1/3 rd rule with h = 0.1.

Module -5

19 a) Obtain the value of y(0.1) using Runge-Kutta method of fourth order for the differential Equation dy/dx = -y and y(0) = 1. (Take h = 0.1)

b) Use the method of least squares to fit a straight line y = ax + b for the following data:

х	1	2	3	4	5
у	6	7	9	10	12

20 Solve by Gauss-Siedel method correct to 3 decimal places.

10x - 5y - 2z = 3, 4x - 10y + 3z = 3, x + 6y + 10z = 3